Overeducation, skills and wage penalty: Evidence for Spain using PIAAC data

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The literature on educational mismatches finds that overeducated workers suffer a wage penalty compared with properly educated workers with the same level of education. Recent literature also suggests that individuals' skill heterogeneity could explain wage differences between overeducated and properly matched workers. The hypothesis is that overeducated workers earn less due to their lower competences and skills in relative terms. However, that hypothesis has been rarely tested due to data limitations on individuals' skills. The aim of this paper is to test the individuals' skill heterogeneity theory in Spain using microdata from PIAAC, because it is one of the developed countries supporting the highest overeducation rates and where its adult population holds the lowest level of skills among a set of developed countries. Our hypothesis is that the wage penalty of overeducation in Spain is explained by the lower skill level of overeducated workers. The obtained evidence confirms this hypothesis but only to a certain extent as skills only explain partially the wage penalty of overeducation.

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1. Introduction

There is a remarkable consensus on the effects of educational mismatch on wages using the standard ORU specification (Duncan and Hoffman, 1981). On the one hand, undereducated workers benefit from a wage premium compared to well-educated workers with the same level of education. On the other hand, overeducated workers earn more than their properly educated co-workers, but earn less than they would at a job requiring their level of education. So, while undereducated workers earn more than their properly matched co-workers experience a wage penalty.

One of the proposed theories to explain overeducation's wage penalty is based on the assignment theory (Sattinger, 1993). It considers that workers' productivity is limited by their job characteristics. So, overeducated workers may thus underutilize their skills, and, in consequence, they are less productive and obtain lower wages than well-educated workers with the same level of education. Following that idea, overeducation may imply overskilling. However, empirical evidence shows a weak correlation between both variables, which means that the assignment theory does not seem to be supported by data (Allen and van der Velden, 2001; Green and McIntosh, 2007).

A supported alternative theory is based on the existence of individuals' skill heterogeneity. From such a perspective, the wage penalty associated to overeducation is due to the huge variation of skills between workers with the same level of education. Then, overeducated workers would not suffer a wage penalty. In fact, they would earn lower wages as a result of their lower skills. If this hypothesis holds, the wage penalty will disappear once individuals' skill level is included in the analysis. However, most of the literature does not explicitly test this hypothesis due to data limitations regarding individuals' skill levels.

In this paper we take advantage of the recently available database of the OECD Programme for the International Assessment of Adult Competencies (PIAAC) because it includes information about individual skills from proficiency test's scores. It allows testing whether individuals' skill heterogeneity could explain the effects of educational mismatch on wages.

We focus on the Spanish case because it has some interesting features that justify the analysis. It is a developed country supporting one of the largest percentages of overeducated workers (OECD, 2013a), a feature that was also observed before the current economic crisis (OECD, 2009; and Verhaest and van der Velden, 2013). At the same time, the Spanish population¹ has one of the lowest levels of proficiency in literacy and numeracy skills (OECD, 2013a).

Therefore, the specific aims of the paper are twofold:

1) Test whether the assignment theory is supported or not by the Spanish data. With this aim we will perform a statistical analysis of the correlation between both educational and skill mismatches.

2) Test the individuals' skill heterogeneity theory in Spain. Our hypothesis is that the wage penalty associated to overeducation could be explained by their lower skill levels. In consequence, overeducated workers may not be suffering a wage penalty in Spain, but their earnings are determined by their skill level.

Our results show a weak correlation between educational and skill mismatches, as it is found in other analyses. Thus, the assignment theory does not seem to be supported by Spanish data. We also find that individuals' skill heterogeneity only explains 18% of the effect of educational mismatch on wages in Spain. The wage penalty still remains for those overeducated workers who are not less skilled than properly matched workers.

The rest of the paper is structured as follows. First, section 2 provides a literature review on the analysis of skills in educational mismatch. Section 3 introduces the PIAAC data and explains how educational and skills mismatch are measured. Section 4 shows the relationship between overeducation and overskilling. Section 5 quantifies the wage penalty of overeducation and the impact of skills using different specifications. Section 6 concludes with some final remarks.

¹ Along with Italy (OECD, 2013a)

2. Literature review

Different theories have been considered in order to explain the overeducation phenomenon (see Leuven and Oosberbeek, 2011 and Quintini, 2011 for a review). However, the most frequently regarded are the assignment model and individuals' skills heterogeneity.

The assignment theory (Sattinger, 1993) makes the assumption that human capital returns depend on both the workers' human capital and the match between the worker and the job. From such a perspective, workers' productivity is limited by their job characteristics. So, overeducated workers may underutilize their skills and, in consequence, they are less productive and obtain lower wages than well-educated workers with the same level of education. Following that idea, overeducation may imply overskilling – or broadly speaking, educational mismatch may imply skill mismatch.

Thanks to the availability of recent databases providing questions relative to skill mismatch, the assignment theory has been explicitly tested. Skill mismatch has been measured by means of subjective workers' responses about whether they consider that their skills are used enough in their jobs. Following the specification developed by Verdugo and Verdugo (1989), different studies have included dummy variables for both educational and skill mismatch in the empirical analysis (Allen and van der Velden, 2001; Di Pietro and Urwin, 2006; Green and McIntosh, 2007; Sánchez-Sánchez and McGuiness, 2013; Mavromaras et al. 2013). It has been found that overeducation and overskilling have both a negative and statistically significant effect on earnings within the same level of education, the overeducation effect being much higher than the overskilling effect. This result underlines that wage penalization associated with overeducation is not explained by under-utilization or waste of workers' skills, whereas the assignment theory is not supported by the results. They may suggest the existence of heterogeneity of workers' skills. However, they do not explicitly test this theory due to a lack of information about workers' skill level rather than skill mismatches.

Specifically, the heterogeneous skills theory takes into account human capital differences between workers. It considers that workers' productivity depends on the human capital level acquired, regardless of job characteristics. Therefore, the observed wage differences among overeducated and undereducated workers compared to well-matched workers with the same educational level may only reflect individual differences in human capital within educational levels. In other words, overeducated workers may be less productive because they have less human capital, not because their job imposes limitations on their productivity.

As has been mentioned before, data availability on workers' skill levels is very limited, whereas different approaches have been considered in empirical analysis to attempt to control for individual skill heterogeneity in the wage equation estimation.

One approach involves the consideration of panel data sets in order to control for all unobserved individual fixed effects (Bauer, 2002; Frenette, 2004; Korpi and Tåhlin, 2009; Tsai, 2010). They find that the wage penalty associated with being overeducated falls dramatically and even disappears when it is estimated by fixed effects, suggesting that (part of) the effect of educational mismatch is caused by unobserved individual ability.

Instead of using a longitudinal framework, Chevalier (2003) analyses cross-sectional data. He creates a proxy of workers' unobserved productivity taking the difference between the estimated and the observed earnings in their first job. In this case, after accounting for the unobserved heterogeneity, the wage penalty for overeducation is slightly reduced. Using a similar methodology, Chevalier and Lindley (2009) arrive at analogous results. They construct a measure of unobserved ability as the residual from a first-job earnings equation, capturing all individual's observed characteristics including job characteristics that affect wages. These residuals should then be a proxy for all time-invariant unobservable characteristics. Chevalier (2003) also introduces a new approach overlapping overeducation and workers' job satisfaction. He divides overeducation into two categories: 'apparent' overeducation, composed of satisfied graduate workers; and 'genuine' overeducation, consisting of dissatisfied graduate workers. Results show that 'genuine' overeducation brings a much larger pay penalty than 'apparent' overeducation.

Following this approach, Green and Zhu (2010) find similar results. They also consider different types of overeducation but use a direct measure of skills. Korpi and Tåhlin (2009) also include explicit indicators of ability in an analysis of Sweden using panel data, and the effect of overeducation on wages still remains statistically significant.

The recent study of Levels et al. (2013) also includes individuals' skill level in the analysis using PIAAC data. They analyse the effect of workers' skills level on the effect of educational mismatches derived from ORU specification for different OECD countries. They find that a considerable part of the effect of educational mismatches on wages can be attributed to skill heterogeneity, but it still remains statistically significant.

In summary, empirical evidence does not seem to support the assignment theory, given that there is a weak relation between educational and skill mismatches. The individuals' skill heterogeneity theory seem to be the most supported explanation for the observed wage differences between overeducated and properly matched workers.

Although there is a wide literature analysing the impact of overeducation on wages in Spain (see Alba-Ramírez, 1993; Murillo et al. 2012; Nieto and Ramos, 2013; among others), to our knowledge, no extensive analysis has tested the role of individuals' skill level on educational mismatch focusing on the Spanish case.

3. Data sources and variable definition

3.1. PIAAC database

The Programme for the International Assessment of Adult Competencies (PIAAC) is a survey which has been conducted by the OECD. It assesses the proficiency of adults from age 16 onwards in literacy, numeracy and problem solving in technology-rich environments. In addition, the survey collects a range of information on reading, writing and numeracy-related activities of respondents, as well as education, labour and family background variables. It was conducted in 24 countries (22 OECD countries) between 2011 and 2012.

Participation in the problem-solving domain was optional, and Spain (and other countries) did not participate in it. As a consequence, the competences we analyse are related to literacy and numeracy. Specifically, the two domains are defined in the following way:

- Literacy: ability to understand, evaluate, use and engage with written texts to participate in society, to achieve one's goals, and to develop one's knowledge and potential. Literacy encompasses a range of skills from the decoding of written words and sentences to the comprehension, interpretation, and evaluation of complex texts.
- Numeracy: ability to access, use, interpret and communicate mathematical information and ideas in order to engage in and manage the mathematical demands of a range of situations in adult life. To this end, numeracy involves managing a situation or solving a problem in a real context, by responding to mathematical content/ information/ideas represented in multiple ways.

Both literacy and numeracy are measured by 10 plausible values calculated using Item Response Theory (IRT), which are represented on a 500-point scale. The idea is that each individual only responds to a limited number of items in the test. To avoid the assignation of missing values in those items which have not been included in the test, the procedure predicts scores using answers from the test and background questionnaires of similar individuals. It generates a distribution of values for each individual and their associated probabilities, with ten plausible values randomly obtained for each individual. This method prevents bias from estimating the result from a small number of test questions. We also consider the jackknife method (80 replicate weights) implemented in PIAAC to derive standard errors in wage regressions².

Given the high correlation between literacy and numeracy skill level (0.92), we only perform the next analysis using literacy skills. However, we repeat the whole analysis using numeracy skills instead of literacy skills as a robustness check.

We consider two sets of variables. The first one includes variables related to workers' human capital as years of education (derived from levels of education), experience, experience squared, non-formal education, and 10 plausible values test scores in literacy. The second one is composed of other personal, job related and regional variables that are included in the model as controls³. These variables are gender, age, nationality, type of

² See OECD (2013b): Technical Report of the Survey of Adult Skills (PIAAC) for more details about IRT and the Jackknife method.

³ The estimation results for these explanatory variables will not be discussed. A full set of the estimation results is available on request.

contract (full-time/part-time), contact term (temporary/permanent), sector (public/private), economic activity (industry, agriculture, construction, services, non-sale services) and 17 regions.

The initial Spanish sample was composed of 6055 observations. We restrict the sample to employed workers who were not enrolled in education at the time. We drop from the analysis armed forces workers, and participants who did not give some of the information we need to perform the analysis. The final sample was 1928 observations. Table 1 of the Annex shows the descriptive analysis of the variables previously defined.

3.2 Measuring educational and skill mismatches

There are different methods to measure educational mismatch: the objective, the subjective or workers' self-assessment and the statistical or realized matches. All of them have advantages and drawbacks, whereas using either measure method finally depends on the availability of the data (see Hartog, 2000; and Leuven and Oosterbeek, 2011; for a review).

The PIAAC data allows us to measure required schooling using both the worker's selfassessment and the statistical method.

The self-assessment method relies on questions that ask workers about the schooling requirements of their job. The PIAAC questionnaire specifically contains the following questions: *'If applying today, what would be the usual qualifications, if any, that someone would need to get this type of job?''*. Educational mismatch is obtained by comparing workers' answers about required education and attained education. Workers are properly or well-matched when their attained education matches with their jobs' required education. Conversely, overeducated (undereducated) workers have more (less) attained education than required by their jobs.

The statistical method (both mean and mode versions) uses information about workers' schooling and their occupations. Regarding the mean version, the required amount of schooling for a worker is determined by the mean of attained education of all workers holding the same occupation. Workers are then defined to be overeducated or

undereducated if their attained education deviates at least one standard deviation from the mean in their occupation. The mode version measure required schooling from the mode of attained education of all workers holding the same occupation. It classifies overeducated or undereducated workers according to whether their education differs from the mode in their occupation.

Table 1 shows the impact of educational mismatch in Spain using the self-assessment method. About half of workers in Spain have a proper match between their education and occupation. From the remaining workers, the PIAAC data highlights that overeducation is affecting 35.63%, 3.8 being the average number of surplus years of education. On the other hand, undereducation concerns the other 15% and their average number of deficit years of education is 3.1.^{4 5}

Table 1: Educational mismatch

	Percentage	Average mismatch in years of education
Undereducation	15.17	3.10 (deficit)
Proper education	49.20	0.00
Overeducation	35.63	3.80 (surplus)

Source: Own elaboration using PIAAC data. Individual sample weights have been considered.

The percentages obtained by the statistical method are shown in Table A.2 of Annex. It is worth noting that different measurement methods were used to report different percentages of educational mismatch, although they are considered to be the same country and the same database. However, the impact on wages is consistent regardless of the measurement method considered (Hartog, 2000). We perform the main analysis measuring educational mismatch using the self-assessment method, and we repeat it using the statistical method as a robustness check.

With regards to the measurement of skill mismatch, we follow the approach defined by the OECD using PIAAC data (Pellizzari and Fichen, 2013; OECD, 2013a). It is a combination of workers' self-assessment questions and their skill proficiency score. The survey asks workers whether they feel they "*have the skills to cope with more demanding duties than those they*

⁴ Although OECD (2013a) measures educational mismatch using the same self-assessment method than us, the percentages of mismatch are different. The reason of those differences is that they cluster education into 4 levels while we take advantage of the maximum level of disaggregation of the data.

⁵ Similar incidence of educational mismatch in Spain has been found by Murillo et.al. (2012)

are required to perform in their current job" and whether they feel they "need further training in order to cope well with their present duties". To compute the OECD measure of skills mismatch, workers are classified as well-skilled in a domain if their skill proficiency score in that domain is between the minimum and maximum score observed among workers who answered "no" to both questions in the same 1-digit occupation (and country). Workers are over-skilled in a domain if their score is higher than the maximum score of self-reported well-skilled workers, and they are under-skilled in a domain if their score is lower than the minimum score of self-reported well-skilled workers.

Individual weighted results show that 72% of workers have a good match between their skills and those required by their jobs. Moreover, overskilling affects 21.4% of workers whereas 6.5% are underskilled.

4. Are overeducated workers also overskilled?

As it has been explained in the previous sections, individuals' skill heterogeneity is one of the explanations of the fact that assignment theory does not seem to be supported by empirical evidence. In other words, most studies have usually found a weak correlation between overeducation and overskilling.

In this section, we analyse the correlation between both educational and skill mismatch (Table 2) to check whether the assignment theory is supported or not using data for Spain. We also compare the distribution of skills between different types of workers to find differences that could suggest the existence of individuals' skill heterogeneity.

The PIAAC data for Spain shows that all workers have a higher probability of being wellskilled, regardless of their education-occupation (mis)match. In particular, we find that 72% of undereducated and 70% of overeducated workers are well-skilled in their jobs. It is surprising that only 7.5% of undereducated workers are also underskilled and 20% have an excess of skills. However, the data shows that 23% of overeducated workers are also overskilled. This results is consistent with Allen and van der Velden (2001) and Green and McIntosh (2007). Indeed, the Pearson chi-square test formally validates the lack of correlation between educational and skill mismatch in Spain⁶.

Table 2: Distribution of undereducated, well-matched and overeducated workers by their skill (mis)match in literacy (in %)

	Underskilling	Proper skills	Overskilling	Total
Undereducation	7.48	72.24	20.28	100.00
Proper education	6.52	73.18	20.29	100.00
Overeducation	6.02	70.62	23.36	100.00

Source: Own elaboration using PIAAC data. Individual sample weights have been considered.

Thus, the empirical evidence for Spain does not seem to support the assignment theory, since educational mismatches are not associated to skill mismatches.

Figure 1 shows the skill level of workers by educational mismatches and by different levels of education in order to provide preliminary evidence existence of skill heterogeneity between workers. It shows that overeducated workers hold a lower skill level than properly educated workers with the same educational level. That fact is repeated for all educational levels (except for bachelor degree). However, undereducated workers tend to have a higher skill level than properly-educated workers with the same educational level (except for upper secondary education).

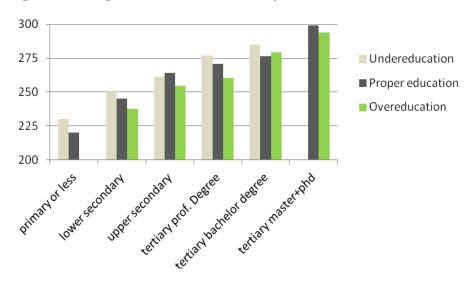


Figure 1: Average skills levels of workers by educational level.

Source: Own elaboration using PIAAC data. Individual sample weights considered.

⁶ The Pearson chi-square test rejects the null hypothesis of non-correlation between variables. Pearson chi2(4) = 4.1182 Pr = 0.390.

Thus, the data show skill heterogeneity between workers with the same level of education. This fact could explain the wage differences between workers according to their educationoccupation match. This is empirically tested in the following sections 4 and 5.

5. Educational mismatch, skills and wages

5.1. Empirical models

In order to quantify the effect of educational mismatch on wages, different specifications based on the traditional wage equation (Mincer, 1974) have been proposed in the literature: the ORU specification developed by Duncan and Hoffman (1981) and the Verdugo and Verdugo (1989) specification. The traditional wage model considers formal education as a proxy of individuals' human capital. However, it is well known that there are components of human capital such as skills or ability. We therefore also include individuals' skills in all three models.

Specifically, the traditional wage equation is defined as follows:

$$[\log(W)]_i) = \alpha + \beta S_i^a + \theta' X_i + u_i$$
(1a)

where $\log(W_i)$ is the logarithm of the hourly wage of worker i; S_i^{a} refers to the number of years of formal education; X_i is a vector of control variables related to personal, job and regional characteristics that also includes other human capital variables such as experience, experience squared and a dummy variable that takes the value of 1 if the worker has participated in some non-formal education activity during the last 12 months prior to the survey and 0 otherwise. Finally, w_i is the error term with zero mean and constant variance.

Including the individuals' proficiency skills (skills_i), the modified model is then defined as:

$$[\log(W]_i) = \alpha + \beta S_i^{\alpha} + \gamma skills_i + \theta' X_i + u_i$$
(1b)

where *skills*_i is a continuous variable measured by scores in a 500-point scale. The higher the score is, the higher the individual's skill level.

A variant of the traditional Mincerian wage equation is the ORU (Over-Required-Undereducated) specification created by Duncan and Hoffman (1981). This specification splits years of education $(\mathfrak{S}^{\mathfrak{a}})$ into three variables: years of education required for the job $(\mathfrak{S}^{\mathfrak{r}})$, years of overeducation $(\mathfrak{S}^{\mathfrak{a}})$ and years of undereducation $(\mathfrak{S}^{\mathfrak{a}})$.

Specifically, it holds that $S^{\alpha} = S^{r} + S^{\sigma} - S^{u}$

In this sense, the following is determined:

- $S^{a} = S^{a} S^{r}$ if the worker is overeducated and 0 if otherwise, and
- $S^{u} = S^{r} S^{a}$ if the worker is undereducated and 0 if otherwise.

The ORU equation is then defined as:

$$[\log(W)]_i) = \alpha + \beta_1 S_i^r + \beta_2 S_i^o + \beta_2 S_i^u + \theta' X_i + u_i$$
(2a)

The other variables' definitions are the same as in specification (1a). The interpretation of the coefficients associated with over- and undereducation is compared with well-matched workers in the same job. The usual findings in the literature are $\beta_1 > \beta_2 > |\beta_3|$.

In order to test the individual's skill heterogeneity hypothesis, we also include the variable related to individuals' skills:

$$[\log(W]_i) = \alpha + \beta_1 S_i^r + \beta_2 S_i^o + \beta_2 S_i^u + \gamma skills_i + \theta' X_i + u_i$$
(2b)

The variable $skills_i$ is defined as in equation (1b). If individuals' skills heterogeneity completely explains the wages' effects of educational mismatch, we should get $\beta_1 = \beta_3 = 0$. If this is true, workers' remuneration composed by their education and skills would be determined by the required education and their individual skill level.

Another contribution to the overeducation literature has been defined by Verdugo and Verdugo (1989, henceforth V&V). This model includes dummy variables related to overeducation and undereducation using the Mincerian wage equation.

The V&V equation is defined as:

$$[\log(W]_i) = \sigma_0 + \sigma_1 S_i^a + \sigma_2 OE_i + \sigma_3 UE_i + \theta' X_1 + u_1$$
(3a)

where OE is a dummy variable that takes the value 1 when the worker is overeducated and 0 otherwise, and UE is also a dummy variable that takes the value 1 when the worker is undereducated and 0 otherwise. The coefficients associated with both variables show the average wage effect of being overeducated and undereducated compared with well-matched workers with the same level of education. The usual finding is that overeducated workers have a wage penalization and undereducated workers benefit from a wage premium compared to well-matched workers with the same educational level. That is, $\sigma_2 < 0$ and $\sigma_3 > 0$.

We also extend that model including skill level variable. The extended V&V model is then defined as follows:

$$[\log(W]_i) = \sigma_0 + \sigma_1 S_i^a + \sigma_2 OE_i + \sigma_3 UE_i + \rho_1 skills_i^a + \theta' X_i + u_i$$
(3b)

In the case that the individual's skills heterogeneity theory is valid, we expect that both coefficients associated with overeducation and undereducation are not statistically significant once we control for individuals' skills. If this is so, workers would be remunerated by their attained education and skills level.

5.2. Results

In line with similar studies (see, for instance, Dolton and Vignoles, 2000; and Di Prieto and Urwin, 2006), we control in all the previous specifications for a possible problem of sample selection bias estimating using Heckman two step specification (Heckman, 1979). This procedure takes into account the possibility that employed workers may not be a random subsample of the sample we are considering. The first step estimates the probability of

being employed using a probit equation⁷ (see the results in Table A.3). Then, the probit estimation is used to construct a selection bias control factor, which is included as an explanatory variable in the wage equation⁸.

As we focus on the analysis of the variables related to human capital, we only comment on the results of those variables in the main test. However, it is worth noting that the coefficients associated to control variables are similar to those in the previous literature. Furthermore, it is found that the lambda coefficient is positive and statistically significant for all specifications. Hence, the omission of the information about the probability of being employed in the wage analysis would imply a bias in the results.

Table 3 reports the results from the estimations of the Mincerian wage models specified in equations (1a) and (1b), the ORU models defined in equations (2a) and (2b) and the V&V specifications defined in equations (3a) and (3b).

With respect to the traditional Mincer's models, it is shown that the returns of the variables related to human capital are similar to previous literature findings (column 1). The return of attained education is 6.4% per year. The years of experience in work also has a positive impact on wages, but there is a moment that its positive impact is decreasing. Finally, training activities in non-formal education also has a positive and significant effect on wages (13%).

When individuals' skills are included in the model (column 2), we find a positive statistically significant effect on wages. Specifically, for each skill's score, individuals have a return of 0.14%. The magnitude of the effect of skills may seem small, but it is important to remember that skills are measured by scores in a 500-point scale. Furthermore, the coefficients of the other variables related to human capital (education, experience and non-formal education) are reduced once skills are included.

⁷ The probit equation of the probability of being employed includes as explanatory variables gender, experience, experience squared, years of attained education, immigrant status, number of children, whether individual is living with spouse or not, and regional dummies.

⁸ The variables we use as exclusion restrictions are both number of children at home and whether individual is living with partner or not. Those variables affect the probability of being employed, but do not determine wages.

Regarding the ORU specification defined in equation (2a), we find that the return of required education is higher than the return of attained education. It points out the existence of educational mismatch. Contrary of most of literature, we find that the return of one year of overeducation is lower than the return (in absolute term) of one year of undereducation. In particular, overeducated workers obtain for each surplus year of education a 3% higher salary than well-educated workers in the same job. Undereducated workers obtain a 3.7% lower wage than well-educated workers in the same job.

In order to test the individuals' skill heterogeneity theory, individuals' skills are included explicitly in the ORU model as specified in equation (2b). Skills have a positive and statistically significant effect on wages, but the effects of educational mismatch still remain statistically significant. Thus, for each year of required education, wage increases 7.45%. The coefficient related with years of overeducation falls from 3% to 2.4% and the coefficient for years of undereducation decreases from 3.7% to 3.1%. Indeed, the hypothesis that years of overeducation and years of undereducation are both equal to 0 (ie. $\beta_2 = \beta_3 = 0$) after controlling for skill is rejected at a level of 1% significance. Hence, the obtained results show that individual's skills heterogeneity explains only part of the wage effects of educational mismatch, and therefore our initial hypothesis about the Spanish case is not supported by the data. Specifically, skills only explain 18% of the wage's effect of overeducation and 14% of the effect of undereducation on wages. The obtained results are in line with the analysis of Levels et al. (2013) for a set of OECD countries.

VARIABLES	Min (1a)	(1b)	OR (2a)		V&V	
Mala		(-~)	(2a)	(2b)	(3a)	(3b)
Mala						
	0.208***	0.189***	0.193***	0.179***	0.195***	0.180***
	[0.0224]	[0.0186]	[0.0218]	[0.0185]	[0.0219]	[0.0178]
8	-0.108***	-0.0728**	-0.0728**	-0.0471	-0.0840**	-0.0550
	[0.0357]	[0.0355]	[0.0350]	[0.0339]	[0.0355]	[0.0347]
0 /	0.0617***	0.0529***			0.0706***	0.0627***
	[0.00509]	[0.00482]			[0.00504]	[0.00494]
Required education			0.0715***	0.0642***		
(years)			[0,00520]	[0,005,17]		
			[0.00530]	[0.00517] 0.0243***		
Overeducation (years)			0.0295***			
Undereducation (years)			[0.00657] -0.0361***	[0.00597] -0.0310***		
Undereducation (years)			[0.00919]	[0.00831]		
Overeducation (dummy)			[0.00919]	[0.00051]	-0.158***	-0.151***
Overeducation (dunniny)					[0.0211]	[0.0207]
Undereducation (dummy)					0.123***	0.117***
endereddeadon (ddinniy)					[0.0309]	[0.0253]
Skill level (scores)		0.00144***		0.00111***	[0.0505]	0.00122***
		[0.000291]		[0.000293]		[0.000292]
Experience 0	0.0170***	0.0165***	0.0172***	0.0168***	0.0170***	0.0166***
÷	[0.00393]	[0.00389]	[0.00389]	[0.00383]	[0.00381]	[0.00385]
•	0.000206**	-0.000173**	-0.000246***	-0.000218***	-0.000236***	-0.000207**
	[8.40e-05]	[8.45e-05]	[8.20e-05]	[8.12e-05]	[8.15e-05]	[8.19e-05]
Non-formal education	0.128***	0.120***	0.0974***	0.0934***	0.103***	0.0984***
	[0.0220]	[0.0204]	[0.0213]	[0.0198]	[0.0214]	[0.0202]
Full-time	-0.0379	-0.0307	-0.0512	-0.0449	-0.0520	-0.0452
	[0.0352]	[0.0350]	[0.0350]	[0.0359]	[0.0348]	[0.0358]
Permanent	0.106***	0.0995***	0.0907***	0.0869***	0.0896***	0.0852***
	[0.0265]	[0.0280]	[0.0261]	[0.0276]	[0.0260]	[0.0272]
	0.135***	0.137***	0.151***	0.151***	0.150***	0.150***
	[0.0355]	[0.0376]	[0.0337]	[0.0355]	[0.0338]	[0.0349]
Activity sector	Yes	Yes	Yes	Yes	Yes	Yes
Regions	Yes	Yes	Yes	Yes	Yes	Yes
Lambda mills	0.115**	0.116***	0.0871*	0.0896**	0.0968**	0.0986***
	[0.0512]	[0.0396]	[0.0526]	[0.0406]	[0.0487]	[0.0377]
Constant	0.677***	0.442***	0.692***	0.511***	0.681***	0.483***
	[0.149]	[0.123]	[0.150]	[0.125]	[0.143]	[0.120]
Observations	1928	1928	1928	1928	1928	1928
R-squared	0.392	0.404	0.432	0.438	0.425	0.432
*						
$\frac{H_0: \beta_2 = \beta_3 = 0}{\text{Standard errors in parentheses}}$				23.35***		

Table 3. Estimated earnings functions

Standard errors in parentheses. *Statistically significant at the 10% level. **Statistically significant at the 5% level. ***Statistically significant at the 1% level. Individual sample weights considered. Equations (1b), (2b) and (3b) also take into account the 10 plausible values of skill level and the 80 replications weights in both estimations.

Finally, the results from V&V specifications defined in equations (3a) and (3b) are shown in the last columns of table 4. The effects of both dummy variables related to overeducation and undereducation are in line with previous literature. Overeducated workers suffer a wage penalization compared to well-educated workers with the same level of education while undereducated workers earn higher wages than well-educated workers with the same level of education. Once individual's skills are included in the model (equation 3b), the effects of educational mismatches are very slightly reduced. Specifically, the penalty associated with overeducated workers is reduced from 17.1% to 16.3%. On the other hand, the premium of undereducated workers falls from 13.1% to 12.4%. As found in the results from the ORU specifications, these results do not seem to support the heterogeneity skills theory, since the effects of overeducation and undereducation still remain once skill is controlled for.

To sum up, we find that individuals' skills are important to determine individuals' wages as well as other human capital variables. However, contrary to our initial hypothesis, we do not find that individuals' skills heterogeneity completely explains the effect of educational mismatch on wages. Specifically, the lower skills of overeducated workers only explain 18% of their lower wages compared to well-matched workers with the same level of education.

5.3. Robustness checks

The PIAAC data allows us to perform some robustness checks to validate the previous results.

First, literature shows that the incidence of both overeducation and undereducation could be different depending on the measurement method applied. However, the effects on wages are quite consistent regardless of the measurement method. Besides the selfassessment method, the PIAAC data allows us to measure educational mismatch by means of both versions of the statistical method, the mean and the mode. The results from the ORU specification measuring educational mismatch by means of both statistical methods confirm the main results (Table A.4. of Annex). Specifically, individuals' skills only explain 14% of the wage penalty of overeducated workers in both models.

Second, we use the variable skill level in numeracy instead of skill level of literacy. As we have already notice, both variables are highly correlated, and therefore we decided not to include both together. We also estimate the ORU specifications including numeracy skills instead of literacy skills (Table A.5. of Annex). The results show that the wage penalty of

overeducated workers is reduced but still remains once skills are included. Specifically, individual's skills heterogeneity explains 22% of the wage penalty.

6. Final remarks

The main objective of this paper is to analyse whether individual's skill heterogeneity explains the wage penalty of being overeducated in Spain. Our hypothesis is that the wage penalty associated with overeducation could be explained by the low skill level of overeducated workers, since Spain holds the lowest level of skill among its population. As a consequence, overeducated workers may not be suffering a wage penalty in Spain, and otherwise their earnings are determined by their skill level. Our results show that individuals' skill heterogeneity only explains 18% of the effect of educational mismatch on wages in Spain. The wage penalty of overeducated workers.

There are some policy recommendations associated with the previous results. On the one hand, as part of the effect of overeducation on wages is due to a lack of competence or skills of overeducated workers, educational policy makers should focus on defining the level of competence or skills that should be acquired at each level of education. Indeed, skills should be evaluated at educational institutions in the same way as education.

On the other hand, other measures should be taken into account by policy makers in Spain, since the wage penalty still remains after controlling for individual skills. First, educational institutions should give all the information about the employability of each type of education to students before they start a specialized course. Second, they should also encourage students in entrepreneurship. Self-employment could be a way to overcome the lack of demand for specific workers. Finally, the Spanish government should make an effort to promote the creation of companies that require high-skilled workers to create a production system based on high technologies.

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Annex:

Variable	Mean	Std. Dev.	Min	Max
Log(wage)	2.18	0.50	0.18	4.53
Literacy proficiency	260.07	42.87	78.76	367.19
Numeracy proficiency	256.71	44.50	82.32	380.86
Age	41.32	10.08	16	65
Male	0.55	0.50	0	1
Immigrant	0.13	0.33	0	1
Attained education	12.21	3.43	6	21
Experience	18.45	10.66	0	55
Experience squared	453.88	470.44	0	3025
Non-formal education	0.56	0.50	0	1
Full time job	0.85	0.36	0	1
Permanent contract	0.81	0.39	0	1
Public sector	0.25	0.43	0	1
Agriculture	0.04	0.19	0	1
Construct	0.07	0.25	0	1
Services	0.47	0.50	0	1
No-sale services	0.28	0.45	0	1

Table A.1. Descriptive statistics

Source: PIAAC. Individual sample weights considered. Number of observations 1928.

Variable	Mean	Std. Dev	Min	Max
MODE				
Overeducation	0.3516185	0.4775994	0	1
Proper education	0.3975564	0.4895198	0	1
Undereducation	0.2508252	0.4336005	0	1
Years overeducation	3.3781	1.771671	1	11
Years undereducation	3.599314	1.629411	1	11
MEAN				
Overeducation	0.1409579	0.3480684	0	1
Proper education	0.6873661	0.4636868	0	1
Undereducation	0.171676	0.3771964	0	1
Years overeducation	1.30805	1.07916	0.0111046	4.856499
Years undereducation	1.429313	1.103022	0.1687933	6.62323

Table A.2. Educational mismatch using the statistical method.

Source: Own elaboration using PIAAC data. Individual sample weights considered.

VARIABLES	(1)
Male	0.202***
	[0.0458]
Experience	0.0702***
	[0.00676]
Experience2	-0.00109***
-	[0.000155]
Attained education	0.106***
	[0.00649]
Immigrant	-0.0564
	[0.0673]
Number of children	-0.0674***
	[0.0247]
Living with spouse	0.0158
	[0.0557]
Regional dummies	Yes
Constant	-1.996***
	[0.145]

Table A.3. Heckman's specification first step. Determinants of being employed.

Observations4689Standard errors in parentheses. *Statistically significant at the 10% level. **Statistically significant at the 5%
level. ***Statistically significant at the 1% level. Individual sample weights considered.

	Mod	Mode		Mean	
VARIABLES	(1a)	(1b)	(2a)	(2b)	
Male	0.202***	0.187***	0.209***	0.193***	
	[0.0216]	[0.0181]	[0.0212]	[0.0181]	
Immigrant	-0.0765**	-0.0488	-0.0626*	-0.0362	
-	[0.0352]	[0.0348]	[0.0350]	[0.0336]	
Required education (years)	0.0823***	0.0741***	0.0977***	0.0884***	
	[0.00550]	[0.00547]	[0.00602]	[0.00630]	
Overeducation (years)	0.0431***	0.0369***	0.0720***	0.0618***	
	[0.00662]	[0.00657]	[0.0168]	[0.0158]	
Undereducation (years)	-0.0393***	-0.0330***	-0.0799***	-0.0690***	
v ,	[0.00767]	[0.00714]	[0.0141]	[0.0142]	
Skill level (scores)		0.00118***		0.00123***	
		[0.000284]		[0.000281]	
Experience	0.0161***	0.0157***	0.0148***	0.0147***	
1	[0.00382]	[0.00384]	[0.00340]	[0.00363]	
Experience2	-0.000214***	-0.000187**	-0.000211***	-0.000186**	
1	[8.17e-05]	[8.40e-05]	[7.77e-05]	[8.16e-05]	
Non-formal education	0.102***	0.0976***	0.0978***	0.0928***	
	[0.0220]	[0.0208]	[0.0224]	[0.0212]	
Full-time	-0.0365	-0.0307	-0.0397	-0.0334	
	[0.0340]	[0.0350]	[0.0342]	[0.0360]	
Permanent	0.101***	0.0964***	0.105***	0.0985***	
	[0.0255]	[0.0273]	[0.0252]	[0.0255]	
Public sector	0.130***	0.131***	0.142***	0.141***	
	[0.0348]	[0.0362]	[0.0350]	[0.0365]	
Activity sector	Yes	Yes	Yes	Yes	
Regions	Yes	Yes	Yes	Yes	
Lambda	0.0793	0.0819**	0.0496	0.0610**	
	[0.0511]	[0.0400]	[0.0306]	[0.0264]	
Constant	0.492***	0.309**	0.379***	0.183*	
	[0.147]	[0.120]	[0.123]	[0.111]	
Observations	1928	1928	1928	1928	
R-squared	0.429	0.437	0.429	0.438	

Table A.4. Estimated earnings ORU functions measuring educational mismatch by means of the statistical method (mode and mean).

Standard errors in parentheses. *Statistically significant at the 10% level. **Statistically significant at the 5% level. **Statistically significant at the 1% level. Individual sample weights considered. Column s (1b) and (2b) also take into account the 10 plausible values of skill level and the 80 replications weights in both estimations.

VARIABLES	(1a)	(1b)
Male	0.193***	0.169***
	[0.0218]	[0.0190]
Immigrant	-0.0728**	-0.0424
-	[0.0350]	[0.0336]
Required education (years)	0.0715***	0.0624***
	[0.00530]	[0.00539]
Overeducation (years)	0.0295***	0.0231***
	[0.00657]	[0.00603]
Undereducation (years)	-0.0361***	-0.0310***
	[0.00919]	[0.00830]
Skill level (scores)		0.00131***
		[0.000299]
Experience	0.0172***	0.0163***
	[0.00389]	[0.00386]
Experience2	-0.000246***	-0.000205**
-	[8.20e-05]	[8.19e-05]
Non-formal education	0.0974***	0.0906***
	[0.0213]	[0.0195]
Full-time	-0.0512	-0.0420
	[0.0350]	[0.0360]
Permanent	0.0907***	0.0840***
	[0.0261]	[0.0277]
Public sector	0.151***	0.150***
	[0.0337]	[0.0354]
Activity sector	Yes	Yes
Regions	Yes	Yes
Lambda	0.0871*	0.0908**
	[0.0526]	[0.0412]
Constant	0.692***	0.497***
	[0.150]	[0.123]
Observations	1928	1928
R-squared	0.432	0.441
Standard errors in parentheses. *Stat	istically significant at	the 10% level. **Statistically

Table A.5. Estimated earnings ORU functions using numeracy skills

Standard errors in parentheses. *Statistically significant at the 10% level. **Statistically significant at the 5% level. ***Statistically significant at the 1% level. Individual sample weights considered. Column (1b) also takes into account the 10 plausible values of skill level and the 80 replications weights in both estimations.